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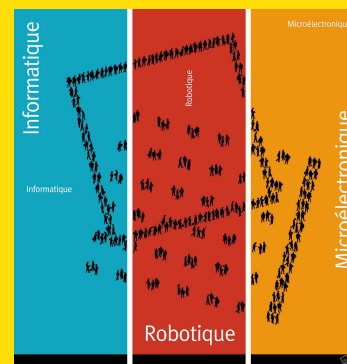
Planning and Fast Re-Planning of Safe Motions for Humanoid Robots: Application to a Kicking Motion

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■ Motivations for Safe Motions

- Initially for paraplegic patients.
- Safe motion in term of constraint-satisfying.
- Accuracy during the movement is not needed.
- Safe motion is more important than performance
- The ZMP or CoP inequality constraint must be continuously satisfied.
- Allows to reinforce the robustness of the controller.



Introduction

- We propose a method based on Interval Analysis guaranteeing the ZMP inequality constraint continuously within the motion duration.
- We will compare experimentally this method with a classical one.
- Kicking motion will be used for illustrating the issue of safe motion planning and re-planning.

■ A method for planning safe motions based on Interval Analysis:

- R.E Moore and F. Bierbaum, *Methods and applications of Interval Analysis*, Soc for Industrial & Applied Mathematics, 1979.
- H. Fang and J.P. Merlet, *Dynamic interference avoidance of 2-DOF robot arms using interval analysis*, IROS 2005.
- L. Jaulin, *Path Planning using intervals and graphs*, Reliable Computing, 2001.
- (Self-Collision avoidance for robot arms, Problem of finding collision-free paths)

■ A new method for generating safe motion and databasing balanced movement:

- S. Lengagne, N. Ramdani and P. Fraise, *A new method for generating safe motions for humanoid robots*, IEEE Humanoid 2008.
- S. Lengagne, N. Ramdani and P. Fraise, *Safe Motion planning for databasing balanced movement of Humanoid Robots*, IEEE ICRA 2009.
- S. Lengagne, N. Ramdani and P. Fraise, *Planning and Fast Re-Planning of Safe Motions for Humanoid Robots: Application to a Kicking Motion*, IEEE IROS 2009.

Motion planning

■ Solving SIP

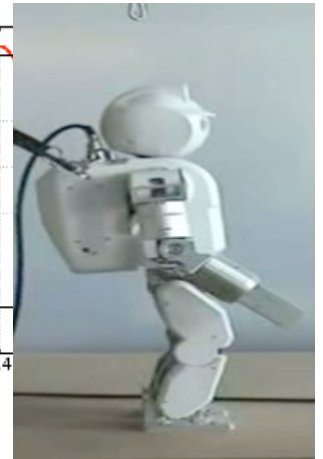
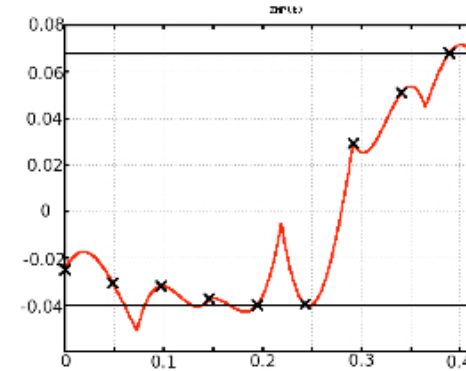
- To be solved, the SIP is transformed into a finite one:

$$\forall i, \forall t_k \in \mathbf{T} \quad g_i(\mathbf{X}, t_k) \leq 0$$

$$\mathbf{T} = \{t_0 = 0, t_1, \dots, t_{N-1}, t_N = T\}$$

- The continuous problem becomes a discrete one.
- Constraint violation.
- How can we ensure the constraint validity ?
- By replacing the time-grid by a time interval discretization.

ZMP(t)



Motion planning

■ Solving SIP by using Interval Analysis:

$$\forall i, \forall t \in [t_0, t_N] \quad g_i(\mathbf{X}, t) \leq 0$$

- We decompose:

$$[t_0, t_N] = [t_0, t_1] \cup \dots \cup [t_{N-1}, t_N]$$

- We compute:

$$\forall i, \forall j \in \{1, \dots, N\} \quad \max g_i(\mathbf{X}, \tau)$$

$$\forall \tau \in [t_{j-1}, t_j]$$

The Guaranteed Discretization Library is available on:
<http://www.lirmm.fr/~lengagne/GDL>

- The interval discretization is done through Interval Analysis.

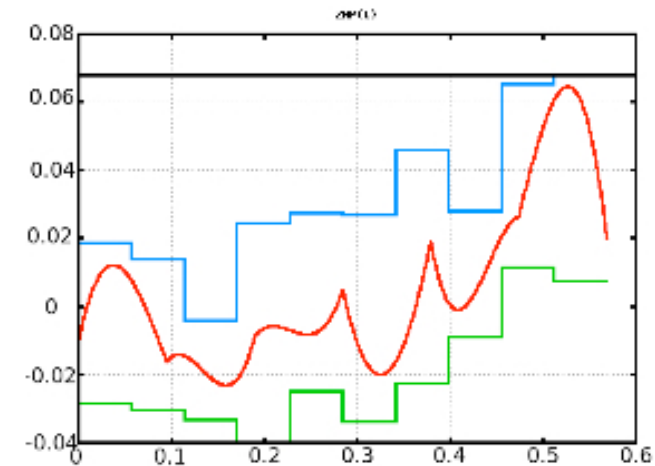


Figure 2: Representation of ZMP(t)

Experimentation on Humanoid Robot

■ Motions

- **Parameters:** $q_i(t) = \sum_{j=0}^{N_s} p_{i,j} \times B_j(t) \mathbf{X} = [T, \mathbf{p}_1, \dots, \mathbf{p}_6]$
 - 5 Coefficients for each dof, the vector X is composed of 61 parameters.

- **Cost Function:** $F(\mathbf{X}) = \int_0^T dt = T$

- Minimum time

Motion Planning method	Classical	Safe
Minimum time	8s	90s
Minimum energy	39s	168s

- **Equality constraints:**

- 12 equality constraints for defining the position and orientation of the flying foot at the beginning and at the end of the motion.

- **Inequality constraints:**

- 76 continuous constraint functions:

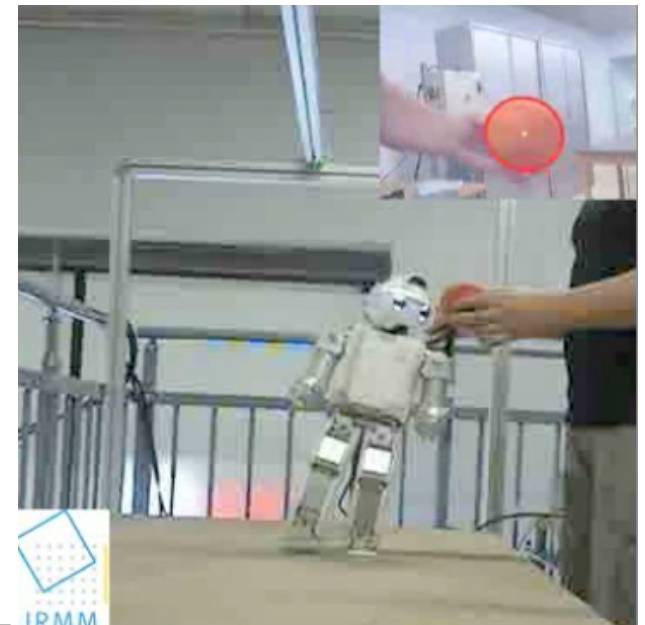
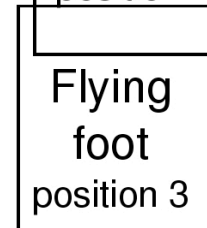
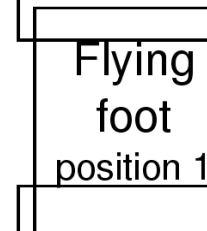
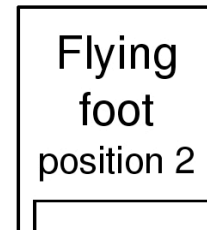
- Each one is decomposed as:

$$\underline{y} \leq y(t) \leq \bar{y} \equiv \begin{cases} \underline{y} - y(t) \leq 0 \\ -\bar{y} + y(t) \leq 0 \end{cases}$$

$$\left\{ \begin{array}{l} \underline{q} \leq q(t) \leq \bar{q} \\ \underline{\dot{q}} \leq \dot{q}(t) \leq \bar{\dot{q}} \\ \underline{\Gamma} \leq \Gamma(t) \leq \bar{\Gamma} \\ \underline{ZMP}_s \leq ZMP_s \leq \overline{ZMP}_s \\ \underline{ZMP}_f \leq ZMP_f \leq \overline{ZMP}_f \end{array} \right.$$

Experimentation on Hoap3

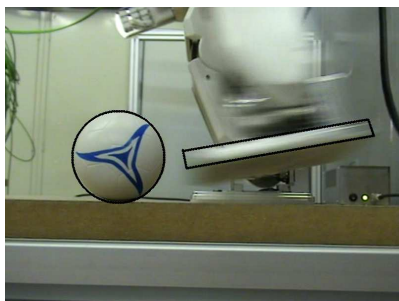
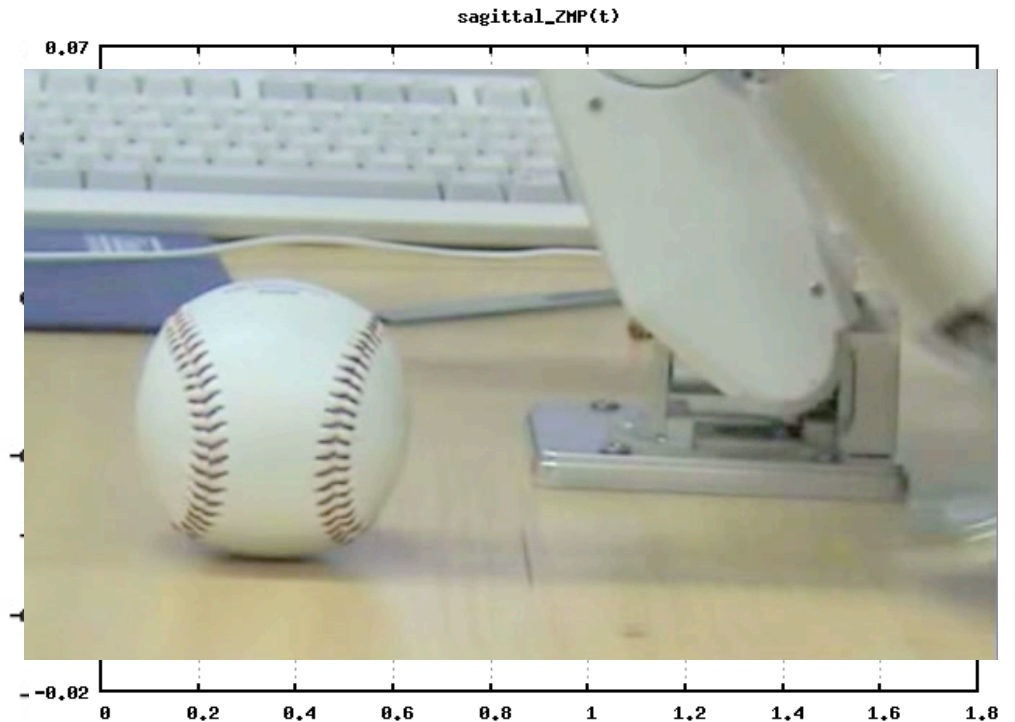
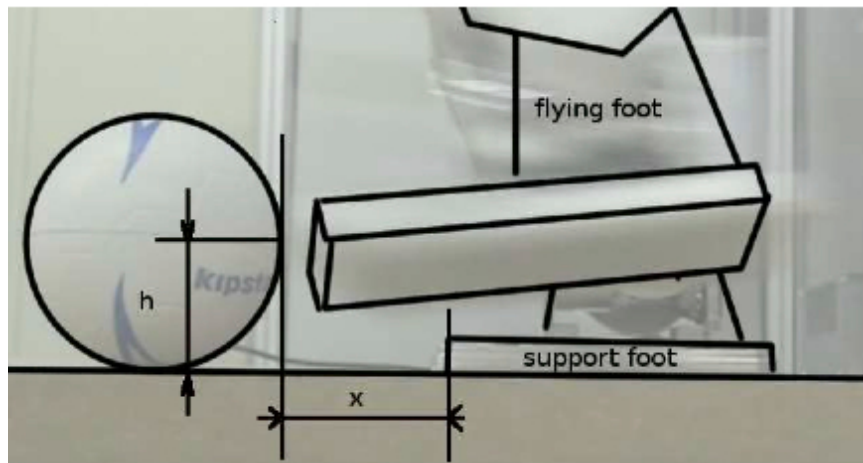
- Creating database to walk.
- Hoap3 experimentations ($l=7\text{cm}$)
- We use three motions:
 - Start motion (1 to 2)
 - Cycle motion (3 to 2)
 - End motion (3 to 1)



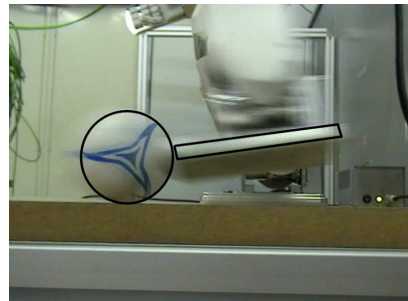
Optimal Kicking Motion

■ Kicking Motion

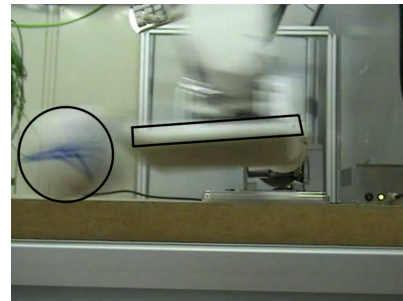
- $V=0,6\text{m/s}$ $x=1\text{cm}$, $h=3\text{cm}$



Before collision



Collision



After collision

How to adapt the kicking motion?

If $x \neq 1\text{cm}$?

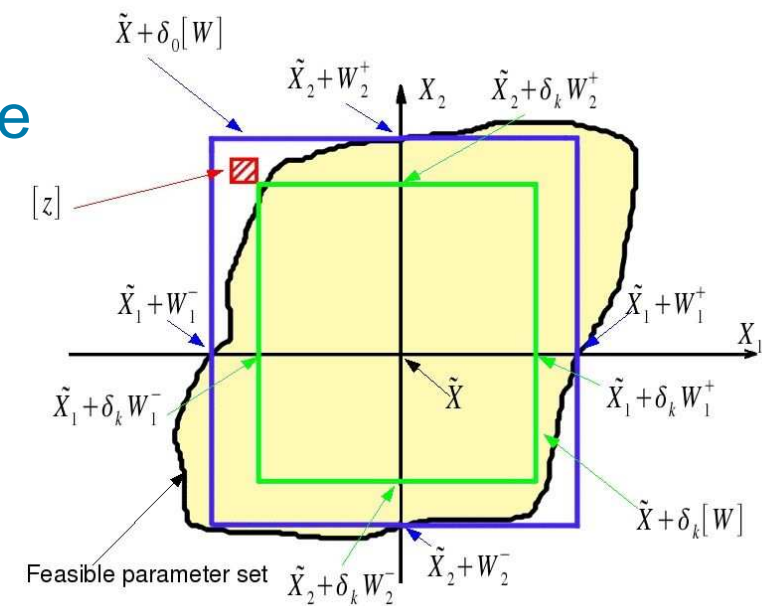
Fast Re-Planning

■ Computation of the feasible subset

- Satisfying all the inequality constraints
- Inner approximation of it
- We define a box as large as possible

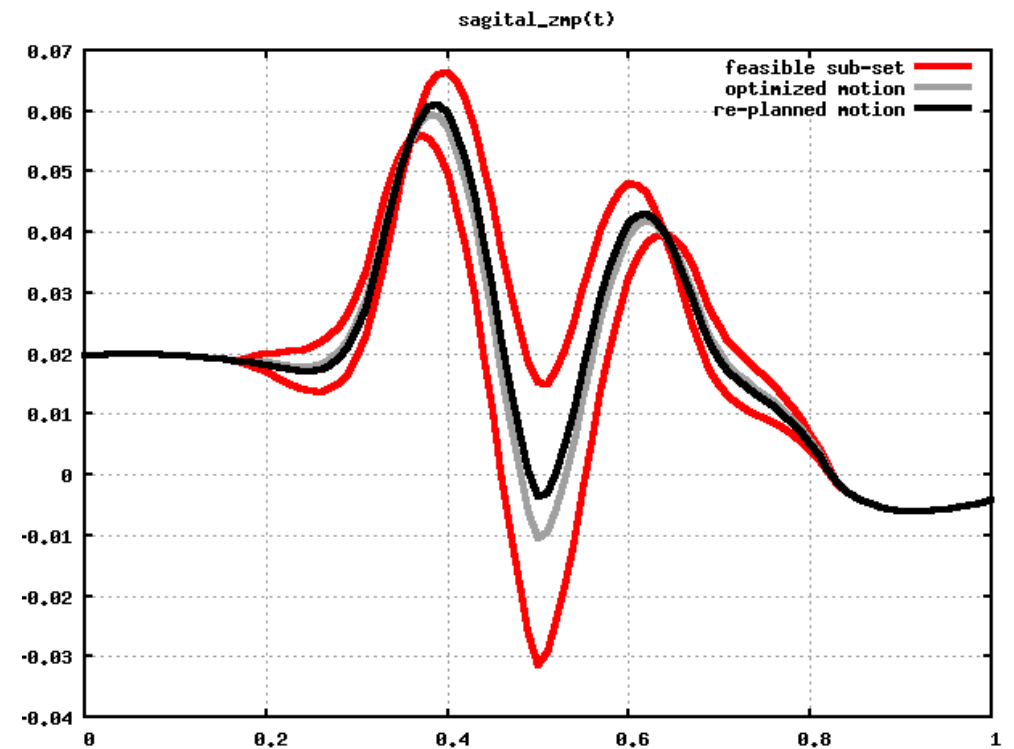
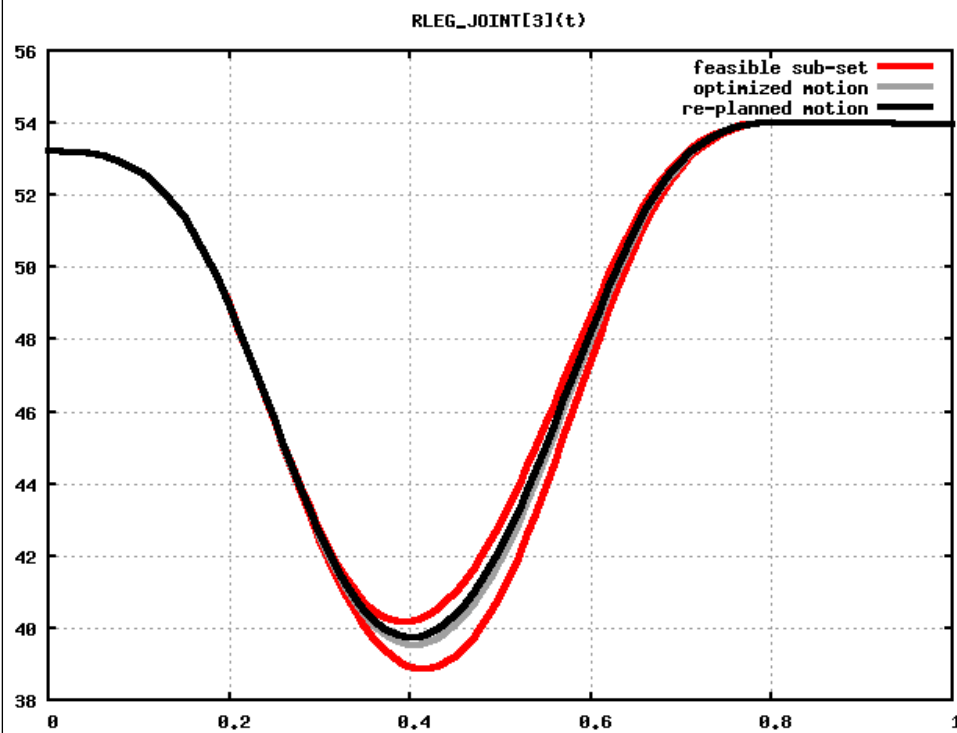
Re-Planning for $h=3\text{cm}$ and $x=1,5\text{cm}$

position	\tilde{X}_i	\hat{X}_i
Right Hip Pitch	-22.60	-21.90
Right Knee	39.68	40.17
Right Ankle Pitch	-17.33	-18.82
Left Hip Pitch	-17.12	-18.12
Left Knee	19.56	19.21
Left Ankle Pitch	4.51	5.34

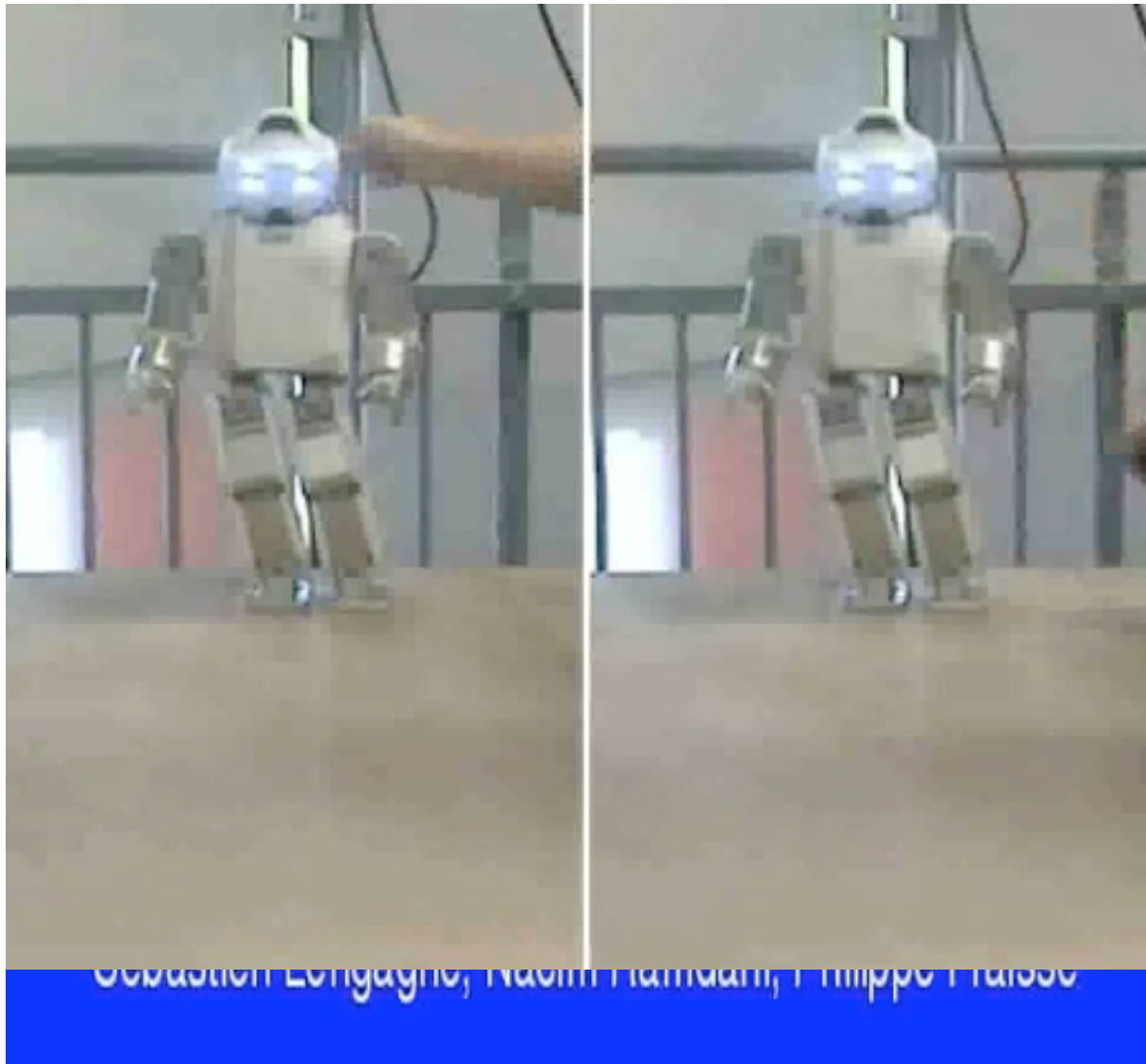


$T_c < 1$ second

Fast Re-Planning



Experimentations



Conclusion and ongoing work

- Time-grid discretization can lead to any constraint violation.
- It improves the balance during the movement.
- Motion re-planning for adapting movement to unexpected events (ex: kicking motion)
- This method has been experimentally validated. Useful for specific movements.
- Embedded applications on small humanoid robot should benefit of this approach.
- The next objective will be to study the aspects of safe motion planning for multi-contact.